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Bayesian and parsimony approaches reconstruct informative trees from simulated morphological datasets

Martin R. Smith

*Department of Earth Sciences, Lower Mount Joy, Durham University, Durham, DH1 3LE, UK; martin.smith@durham.ac.uk*

Phylogenetic analysis aims to establish the true relationships between taxa. Different analytical methods, however, can reach different conclusions. In order to establish which approach best reconstructs true relationships, previous studies have simulated datasets from known tree topologies, and identified the method that reconstructs the generative tree most accurately. On this basis, researchers have argued that morphological datasets should be analysed by Bayesian approaches, which employ an explicit probabilistic model of evolution, rather than parsimony methods – with implied weights parsimony identified as particularly inaccurate.

Accuracy alone, however, is an inadequate measure of a tree’s utility: a fully unresolved tree is perfectly accurate, yet contains no phylogenetic information. The highly resolved trees recovered by implied weights parsimony in fact contain as much useful information as the more accurate, but less resolved, trees recovered by Bayesian methods. By collapsing poorly supported groups, this superior resolution can be traded for accuracy, resulting in trees as accurate as those obtained by a Bayesian approach. In contrast, equally weighted parsimony analysis produces trees that are less resolved and less accurate, leading to less reliable evolutionary conclusions.

*Keywords*.—phylogenetic inference; parsimony analysis; equal weights; implied weighting; Bayesian phylogenetic methods; information content

# Introduction

Evolutionary history can be reconstructed using parsimony-based or probabilistic approaches. Because models used with molecular datasets generally share a common probabilistic construction, statistical methods can be used to determine the most appropriate model [1]. With morphological datasets, however, it is more difficult to establish whether probabilistic models or parsimony better reconstruct phylogenetic relationships (which are typically unknown).

A pragmatic approach to this question is to simulate data from a known tree. With the important caveat that generative trees and simulated morphological datasets may be unrealistic [2,3], probabilistic approaches typically reconstruct the generative tree most accurately (i.e. with least conflict), followed by parsimony under equal and implied weights in turn [4–9].

Previous studies have advocated accuracy as the sole criterion by which to select a method [5–11]. Congreve & Lamsdell [9] (problematically [2]) define the most accurate tree as the one that bears the fewest of incorrect splits. Other authors [5–8,11] use the Robinson-Foulds distance as a proxy for accuracy (even though the RF distance is also influenced by precision; a pair of trees can be made two units more similar by replacing an incorrect partition with a correct one, or by collapsing two incorrect partitions.) Goloboff et al. [2] propose alternative tree similarity metrics as proxies for accuracy.

Accuracy alone, however, is not the only goal when reconstructing trees [11]. No tree shows less conflict than a single polytomy, for a total absence of relationship information guarantees that no relationship is incorrectly resolved. An emphasis on accuracy therefore disadvantages methods that produce highly resolved trees [11] (and *vice versa*). Naturally [12], more accurate methods consistently yield less resolution [2,5,7,8,11].

This trade-off has been acknowledged by collapsing groups whose support is below an arbitrary value [2,6,8,11], which sacrifices resolution in order to improve accuracy—but despite acknowledging the role of resolution, these studies still treat accuracy as synonymous with performance.

We should instead favour methods that recover as much *information* as possible about the true tree, striking a balance between accuracy and resolution. For example, a tree that resolves 20 relationships conveys much information about the correct tree, even if one of those relationships is incorrect; a tree that resolves just one relationship conveys less information, even if that single relationship is correct. By the same measure, if two trees are equally accurate, then the more precise contains more phylogenetic information: accuracy and resolution are two complementary ways that a tree can be useful, and our objective should be to maximise both [12]. Here I explore whether previous conclusions hold up if trees are evaluated according to their overall similarity (in terms of shared information) rather than ‘accuracy’ alone.

# Methods

Congreve and Lamsdell [9; CL hereafter] simulated 55-character matrices from a bifurcating 22-tip tree using a Markov *k­*-state 1 parameter model with rates sampled from a discretized Gamma distribution. Their generative tree is the single most parsimonious tree obtained from a study of Ordovician trilobites; its edges were assigned a unit length.

O’Reilly *et al.* [5; OR hereafter] simulated matrices containing 100, 350 and 1000 characters from a bifurcating 75-tip tree using a modified HKY85 model; they followed a previous simulation study [4] in selecting a single bifurcating tree from a morphological + molecular analysis of Lissamphibia.

I used TNT [13] to conduct parsimony searches on each of these matrices under equal and implied weights, using the parsimony ratchet and sectorial search heuristics (search options: xmult:hits 20 level 4 chklevel 5 rat10 drift10). I took a strict consensus of all optimal trees obtained under equal weights, and under implied weights [14] at the concavity constants used in each respective study (CL: *k* = 1, 2, 3, 5 and 10; OR: *k* = 2, 3, 5, 10, 20 and 200). For each dataset I generated a further strict consensus of all trees that were optimal under any of the concavity constants, excluding the unreasonable value of *k* = 1, which inadequately penalises extra steps beyond the first, and thus exhibits undesirable properties of clique analysis [15] (see Supplementary Text).

I also generated majority-rule consensus trees in MrBayes 3.2.2 [16] using an Mk model, with rates distributed according to a gamma parameter. I combined results from four independent runs, each of which employed four Metropolis-coupled Markov chains. After a burn-in period of 4 000 000 generations, the cold chain in each run was sampled every 10 000 generations for 6 000 000 generations. The sampled topologies faithfully reflected the posterior distribution for each dataset (0.999 < PSRF < 1.001; ESS > 400).

To explore the relationship between resolution and accuracy, I generated further trees for each analysis by collapsing poorly supported groups. Under the Mk model, I collapsed groups whose posterior probability was < 95%, 90%, 85%, … 50%. In parsimony analyses, I compared different measures of node support. Under Jackknife and Bootstrap resampling, I collapsed groups with (i) absolute frequency supports of < 0%, 2%, 4% … 100%; (ii) relative frequency (GC) support of < -100%, -95%, … 95%, 100%. Under Bremer support, I collapsed groups with Bremer support values less than 1, 2, 3, … 20 with equally weighted trees (TNT command subopt *x*; bbreak;); under implied weighting, Bremer support values were drawn from a logarithmic distribution (0.730...19, 2.5×10−3→1×100), reflecting the fractional nature of tree scores under implied weights [14].

Symmetric difference metrics calculate how much information two trees hold in common [17] — that is, how much information a generated tree contains about the generative tree. Where the generative tree is bifurcating, a particular relationship may be resolved the same way (*s*) or a different way (*d*) on each tree, or resolved in the comparison tree only (*r*) [18,19]. The symmetric difference (‘SD’, also termed the Robinson-Foulds distance) is given by 2*d* + *r*. The symmetric difference is conventionally normalized against the total information present (‘TIP’) in the two trees, 2*d* + 2*s* + *r*[19]. Undesirably, this assigns a fully unresolved tree an equal score to a tree that is perfectly resolved and completely incorrect (Fig. 1a). In the present context, therefore, it is more appropriate to normalize against the maximum information (‘MaxI’) that could potentially have been resolved, 2 (*d + s + r*).

The unit of relationship information may be a quartet (a four-taxon statement) [18–20] or a bipartition split [21–23]. (Each clade in a tree corresponds to a bipartition that splits taxa into ‘members’ and ‘non-members’.) Partitions offer a simple but incomplete measure of the relationship information accommodated in a tree. For example, the trees ((A, (**X**, B)), (C, D)) and ((A, B), ((C, **X**), D)) have no partitions in common, even though they both contain the same information regarding the relationships between (A, B) and (C, D). As a consequence, the partition difference (= Robinson-Foulds distance) suffers four essential shortcomings [21]. Firstly, it is imprecise; the number of unique values that the metric can take is two less than the number of taxa. Simply put, a more precise method can more readily allocate similar trees distinct difference values, where a less precise method would assign them the same score. Secondly, it is rapidly saturated; relatively small differences can result in the maximum distance value, particularly in asymmetric trees. Thirdly, its value can be counterintuitive; for example, moving a single tip to a particular location can generate a higher difference value than moving both that tip and its immediate neighbour to the same point (Supplementary Text). Fourthly, its value depends on the symmetry of the underlying tree, with balanced trees containing proportionally more uneven partitions and thus attracting lower average distances (a factor possibly overlooked by [7]; see Supplementary Text).

Quartets, in contrast, completely represent all topological information within a tree. The quartet dissimilarity measure is precise, does not rapidly reach saturation, generates a meaningful value for random trees, is robust to the placement of wildcard taxa, and consistently increases in value as trees become more different; and every quartet represents an equal quantity (one trit) of information. I consider it to represent a more useful, meaningful and readily interpreted indicator of tree similarity.

I calculated quartet distances using the QuartetStatus function in the new R package Quartet [24], which employs the tqDist algorithm [25]. Partition distances were calculated using the Quartet function SplitStatus. To summarise results, *s*, *d*, and *r* were calculated for each individual tree relative to the generative tree, and the mean of each of parameter was calculated at each resolution in each analysis.

Previous studies (e.g. [5,6]) have presented plots of unnormalized symmetric difference against resolution as depicting accuracy against precision. The unnormalized symmetric difference, however, is a function of both resolution and accuracy. A change in resolution (*x*) necessarily influences the value, and the range of possible values, of the symmetric difference (*y*). Because the axes are not independent, t I instead plotted the proportion of quartets or partitions that are the same in both trees (*s*), different in both trees (*d*), and only resolved in the generative tree (*r­*) on ternary plots using the Ternary R package [26], oriented such that SD/MaxI decreases vertically, and resolution decreases horizontally (Figure 1a). This plotting configuration distinguishes the relative contributions of resolution and accuracy (whether in terms of the number of proportion of errors) to overall similarity (Figure 1b).

All data, scripts and analyses used in this study are archived on GitHub [27,28].

# Results

Ideally, measures of node support would assign incorrect nodes low support values. With the CL datasets (55 characters, 22 tips), resampling methods accomplished this more effectively than Bremer support (Figure 1c,d), substantiating concerns about the suitability of this metric [29,30]. By the same measure, the groups contradicted/supported (GC) metric outperformed group frequency (as anticipated by [31]), and bootstrap resampling outperformed the jackknife approach (contra [32]). This said, differences between the methods were not statistically significant (Supplementary Text). Subsequent analyses employed the Bootstrap GC metric.

With the CL datasets, there is no significant difference (at *p* = 0.01) between the MaxI-normalized quartet symmetric difference of the best trees generated by the *Mk* model or implied weights (*k* ∈ {2, 3, 5, 10}) – but the best trees generated by equal weights, implied weights with *k* = 1, and the consensus of *k* values are significantly worse than those produced by the other methods (Figure 2a; Supplementary Text).

Collapsing the least-supported groups initially increases the overall accuracy (as predicted in [2,33]), leading to a slight increase in the overall informativeness of the tree (Figure 2a,b). Beyond a GC score of c. −15, the gain in accuracy no longer offsets the resolution lost; collapsing further groups thus removes ‘correct’ information and reduces the similarity between the tree and the reference tree. Because a Bayesian approach results in less resolution, its most resolved trees cannot generally be improved by collapsing groups (Figures 1c,d, 2).

These results hold even if the (problematic) partition difference metric is employed (Figure 1b), though relatively more groups must be collapsed (those with a GC score of < 10) to maximise this metric. The results do not meaningfully change when datasets with low consistency indices are excluded.

Similar results are observed in the OR datasets (Figure 2c­–e): at any given level of resolution, the best trees obtained by the Mk model are similar in accuracy to those obtained under implied weights (except with very small values of *k*), but are more accurate than those obtained using equal weights.

These datasets also demonstrate the impact of dataset size on tree quality. With larger ratios of characters to taxa (1000 or 350 characters, 75 tips), all methods produced reasonably accurate, well-resolved trees (Figure 2d–e). With the smallest (100 character) datasets (Figure 2c), trees were much more different from the generative tree, and the choice of method influenced results more strongly: the Bayesian approach could obtain substantially less resolution, and implied weights recovered poor trees at low values of *k*. No existing method can overcome the inherent limitation of a low character to taxon ratio.

# Discussion

In the simulation studies analysed herein, parsimony and probabilistic analyses can generate equally informative reconstructions of evolutionary history, if accuracy and resolution are recognized as complementary aspects of information [12]. Parsimony results are most informative when groups with a bootstrap GC value of < −15 are collapsed, and are as accurate as Bayesian results if nodes are collapsed until trees exhibit an equal resolution. As an important caveat, parsimony analysis must employ a moderate weighting scheme. At low values of the concavity constant (*k* < 2, say), implied weights begins to exhibit the undesirable properties of clique analysis, whereas at high values (as *k* → ∞), it converges to the inferior equally weighted parsimony (Supplementary Text). Each of these extremes yields results that are less accurate and less resolved, making them more different from the generative tree and consequently less informative about evolutionary history; results encountered only under such parameters do not merit biological interpretation.

Quite aside from issues with the validity of data simulation protocol [2,3], previous results that favour Bayesian methods over parsimony [5–8,10], or equal weights over implied weights [9], have arisen because accuracy has been considered the sole measure of a method’s performance. Future simulation studies should evaluate methods based on normalized tree similarity metrics that reflect the total *information* contained within two trees – a quantity that reflects both resolution and accuracy. In the analyses examined herein, neither Bayesian nor parsimony analyses generate consistently superior results. Of course, other factors may influence a researcher’s choice of methods: Bayesian models, for instance, can readily integrate non-morphological data [34,35] and allow probabilistic hypothesis testing using Bayes Factors [36]. Such considerations notwithstanding, researchers may wish to explicitly compare the results of both Bayesian and implied weights analyses when conducting phylogenetic analysis; observations common to both approaches and receiving strong node support values are particularly likely to be well supported by underlying data.

# Figure legends

**Figure 1. Method selection.** (a), normalizing the symmetric difference against the total information present in two trees (SD/TIP, dotted lines) fails to identify a completely incorrect bifurcating tree (all relationships resolved differently; bottom corner) as more misleading than a polytomy (all relationships unresolved; rightmost corner). Random trees (coloured line) with more relationships resolved receive better scores, as some relationships will by chance be resolved correctly. Normalizing against the maximum possible relationship information (SD/MaxI, solid lines) ensures that misinformation is penalized over non-information; as such, random trees with more relationships resolved (which thus contain more misinformation) receive worse scores. (b), four measures of tree quality, each rewarding different tree properties. (c–d), impact on tree quality when least-supported groups are collapsed: (c), counting quartets; (d), counting partitions.

**Figure 2.** **Status of quartets and bipartitions in trees recovered from simulated datasets.** Points denote the average number of quartets (a, c–e) or partitions (b) that are the same as the generative tree, resolved differently to the generative tree, or not resolved. Each series indicates the effect of progressively collapsing the least-supported groups in trees generated by analysis of CL (a–b) and OR datasets (c, 100 characters; d, 350 characters; e, 1000 characters) under the specified analytical parameters. An increase in the vertical direction corresponds to a decrease in normalized symmetric difference (i.e. more similar / informative trees); an increase in the horizontal direction corresponds to a decrease in tree resolution.

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# Author contributions

MS is the sole author.

# Data accessibility

The Quartet package will be available from the CRAN repository when the review process is complete. **Data and analyses** available on GitHub and archived on Zenodo. CL: <https://github.com/ms609/CongreveLamsdell2016> [27]; OR: <https://github.com/ms609/OReillyEtAl2016> [28].

Electronic Supplementary Material accompanies the article:

* **Supplementary Text** (PDF, Rmd): includes a detailed comparison of the suitability of tree comparison metrics, and discusses the use of small concavity constants in implied weighting. The Rmd file provides the source R code used in analyses, to enable the reproduction of research results. These files accompany the online article at [URL of published article]

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# Ethical statement

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